

Fig. 5. Glass electrode emf shifts at 22°C produced by pressure (1000 kg.cm⁻²) in bicarbonate, carbonate buffers, and sea water at $\mu = 0.75$, as a function of pmH = $-\log m_{\rm H}$ measured at atm pressure. Curve 1, NaHCO $_3$, Na $_2$ CO $_3$, CO $_2$ ([HCO $_3$ -] + [CO $_3$ -] 0.05 — 0.09 and 0.0025 (arrow) in 0.5 NaCl. Curve 1', KHCO $_3$, K_2CO_3 , CO_2 ([HCO₃⁻] + [CO₃⁻] 0.05 - 0.09) in 0.5 KCl. Curve 2, NaHCO₃, Na₂CO₃, CO₂ ([HCO₃ $^-$] + [CO₃ $^-$] 0.05 $^-$ 0.09) in 0.5 NaCl; effect of Na₂SO₄ (0.030). Curve 3, NaHCO₃, Na_2CO_3 , CO_2 ([HCO_3^-] + [CO_3^-] 0.05 - 0.09) in 0.5 NaCl; effect of MgSO₄ (0.030), MgCl₂ (0.026), CaCl₂ (0.01) (Precipitates are obtained at pH > 8.0). Arrows indicate results for [HCO3-] $[CO_3^{=}] = 0.0025$ (see also curve segments 6). Curve 3', $NaHCO_3$, Na_2CO_3 , CO_2 ([HCO_3^-] + [$CO_3^=$] 0.05 - 0.09) in 0.5 NaCl; SO₄ = effect of MgSO₄ (0.030). Curve 4, NaHCO₃, Na_2CO_3 , CO_2 ([HCO $_3$ ⁻] + [CO $_3$ ⁻] 0.05 - 0.09 and 0.025 (arrows); effect of MgCl2 (0.056). Curve 5, Natural sea water Cl $\%_{
m o} \simeq$ 19.5 (Atlantic), corrected at C1 $\%_{
m o}$ 20.0 (μ = 0.75). Curve Natural sea water; SO₄= effect. Curve 6, Artificial sea water: $[HCO_3] + [CO_3^{=}] = 0.0025$; 0.030 MgSO₄, 0.026 MgCl₂, 0.010 CaCl2, 0.5 NaCl (with or without boric acid in the acid range). Curve 6', Artificial sea water with boric acid (4.3 10-4) (alkaline range). Curve 7, Effect of boric acid; smoothed difference in my between ($m{E}_1 - m{E}_{1000}$) in artificial sea water without boric acid (see curves 3 and 6) and $(E_1 - E_{1000})$ in the same with 4.3 10^{-4} boric acid (see curves 6 and 6').

Inspection of curve 1 further indicates that the results at $pmH_1 \leq 7.00$ are identical in KCl and NaCl. If one again assumes that the bicarbonate concentration corresponds to the sum of the free HCO3- ions and the undissociated sodium or potassium bicarbonate, log $k'^{m}_{(1)1000}/k'^{m}_{(1)1}$ is equal to 0.359 ($\Delta E_{1000} = 21.0 \text{ mv}$) at pmH₁ 7.0, 0.376 at pmH₁ 6.0, and 0.385 at pmH₁ 5.0. Here the term 2 log $\gamma_{A_1}/\gamma_{A_p}$ in Eq. [3] is not constant and depends on the buffer ratio.

The question that remains to be answered concerns the choice of suitable values for $pk'_{(1)1000}$ and $pk'_{(2)1000}$ in the pmH₁ range 7.0-8.5, where the emf changes induced by pressure depend on both ionization functions.

If we consider a solution containing NaCl and $NaHCO_3$ at atmospheric pressure, its $pmH_1 = \frac{1}{2}$ $(pk'^{m}_{(1)1} + pk'^{m}_{(2)1});$ at $\mu = 0.75$, one finds $pmH_1 \simeq$ $7.8 = \frac{1}{2} (6.0 + 9.6)$ and $[CO_2] = [CO_3^{=}]$. At $pmH_1 =$ 7.8, $\Delta E_{1000} = 20.0$ mv, and simple considerations show that $[CO_2]$ will remain equal to $[CO_3^=]$ if 2.3 RT/F $\log k'^m_{(1)1000}/k'^m_{(1)1}$ and 2.3 RT/F $\log k'^m_{(2)1000}/k'^m_{(2)1}$ are taken symmetric with respect to $\Delta E_{1000} = 20.0$ mv.

For instance, 21.0 and 19.0 mv read at pmH₁ 7.0 and 8.5 on curve 1 of Fig. 5. In that case the equilibrium $2 \text{HCO}_3^- = \text{CO}_3^= + \text{H}_2 \text{CO}_3$ is shifted. Thus, at $pm \text{H}_1 = 7.8$, if $[\text{HCO}_3^-] + [\text{CO}_3^-] = 0.05$, 6.10^{-5} HCO $_3^-$ is formed at 1000 kg. cm $^{-2}$ at the expense of 3.10^{-5} CO $_2$ and 3.10⁻⁵ CO₃=, which corresponds to a 4% change of the initial CO_2 and CO_3 = concentrations. At pmH_1 7.0 and 8.5, the change of either $[CO_2]$ and $[HCO_3]$ or [CO₃=] and [HCO₃-] is negligible when pressure is applied. If one could assume 2.3 RT/F $\log k'^{m}$ (1)1000/ $k'^{m}_{(1)1}$ and 2.3 RT/F log $k'^{m}_{(2)1000}/k'^{m}_{(2)1}$ to be equal to ΔE_{1000} read on curve 1 at any pmH_1 between 5.0 and 9.0, the CO₂, HCO₃-, CO₃= concentrations would remain constant at any pressure. This is what happens at infinite dilution where $\Delta V^{o}_{(1)1} = \Delta V^{o}_{(2)1}$.

In KCl, if one neglects the slight minimum at pmH1 7.8, 2.3 RT/F log $k'^{m}_{(1)1000}/k'^{m}_{(1)1}$ and 2.3 RT/F log $k'^{m}_{(2)1000}/k'^{m}_{(2)1}$ are equal within \pm 0.25 mv over the range 7.0-9.0. However, this is an oversimplification since the minimum at 7.8 could be explained by the release of $\rm CO_3^-$ and $\rm HCO_3^-$ from ion pairs. $\rm HCO_3^-$ behaves as a base at $pmH_1 < 7.8$ and as an acid at $pmH_1 > 7.8$, whereas the release of CO_3 always results in lowering the hydrogen ion concentration.

The choice of the values of $pk'^{m}_{(1)1000}$ at pmH_1 7.0 and $pk'^{m}_{(2)1000}$ at pmH_1 8.5 to be used in the pmH_1 interval 7.0-8.5 remains questionable, even in KCl, but there is no other alternative unless reliable values for $pk'^{m}(1)$ and $pk'^{m}(2)$ become available in absence of any ionic association. However, at the alkaline end of the pmH_1 interval 7.0-8.5, $pk'^{m}(1)$ needs not to be known with great precision to calculate [HCO3-] or $[CO_3^{=}]$. At pmH_1 8.0, an error of 0.02 ($\Delta E \simeq 1.2$ mv) in pk'^{m} ₍₁₎₁₀₀₀ affects [CO₂] by 2% and [HCO₃⁻] and $[CO_3=]$ by only 0.1%.

The separate salt effect of NaCl on 2.3 RT/F log $k'^{m}_{(1)1000}/k'^{m}_{(1)1}$ can be estimated at $pmH_1 < 5.0$ since curve 1 in Fig. 5 seems to reach a plateau in the acid range and since ΔE_{1000} is known at 0 ionic strength (25.0 mv). Thus, for the salt effect, one finds 25.0 -22.6 = 2.4 mv. This value fits with the fact that $2 \Delta E_{1000}$ = 23.6 mv at μ = 0.75 in a solution containing only NaCl and saturated with CO₂. At $\mu = 0$, 2 $\Delta E_{1000} =$ 26.2 mv (3) and the difference 26.2 - 23.6 = 2.6 mv.

It seems reasonable to assume that the difference between ΔV_{1} found in pure CO_{2} solutions and in bicarbonate buffer at 0 ionic strength might be related to the existence of NaHCO3 ion pairs even when the concentration of NaHCO3 becomes very small. The same effect occurs in other buffer systems investigated with the glass electrode technique: ΔVo1 is always found to be smaller in buffers than in the corresponding pure acid (3), and the explanation given above might be general.

Finally, one will notice (Fig. 5, dotted part of curves 1 and 2) that Corning 015 electrodes display an alkaline error in presence of NaCl at 1000 kg. cm-2 at $pmH_1 > 8.25$, although no such error can be detected even at 8.75 at atmospheric pressure.

Ionization of carbonic acid in presence of Mg++, Ca++, and SO₄= in NaCl solutions, at concentrations found in sea water, at 1 atm and 1000 kg. cm-2 and at different buffer ratios ($\mu = 0.75$).—When Ca or Mg salts are added to carbonate and bicarbonate buffers, it is well known [see Garrels, Thompson, and Siever (12)] that MgCO3 and CaCO3 ion pairs are formed and that the trapping of HCO₃ ions is also to be considered. The dissociation of carbonic acid can still be described by the ionization functions $k'_{(1)}$ and $k'_{(2)}$ where [CO₃=] and [HCO₃-] refer to the free carbonate and bicarbonate ions (plus those bound to Na as seen in the preceding section), but it is also useful to define apparent ionization functions $k''_{(2)} =$ [H+] $[CO_3=]_T/[HCO_3=]_T$, $k''_{(1)}=[H+][HCO_3=]_T/[CO_2]$ where $[CO_3=]_T$ and $[HCO_3=]_T$ correspond to the total amount of carbonate and bicarbonate. We will call $k'_{(2)}$ and $k'_{(1)}$ true ionization functions.

True and apparent ionization functions of carbonic acid in presence of Mg^{++} , Ca^{++} and SO_4^{-} , in NaCl solutions at 1 atm ($\mu=0.75$).—Figure 6 gives the pmH_1 changes (in mv) produced when $MgCl_2$, curve 4; $MgCl_2 + MgSO_4$, curve 3; $MgCl_2 + MgSO_4 + CaCl_2$, curve 2; Na_2SO_4 , curve 1 are added to bicarbonate and carbonate buffers at atmospheric pressure, as a function of pmH_1 measured in the solutions containing the added salts. The reference 0.01 HCl + 0.49 NaCl solution has the same salt composition as the buffer under test it is assumed that $m_{H^+} = m_{HCl}$ and that the mean activity coefficient of HCl is the same in both compartments. The added salts are tested at concentrations normally found in sea water ($Cl\%_0 = 20.0$).

Effect of SO_4 ⁼ on the true ionization functions $k'_{(1)1}$ and $k'_{(2)1}$.—Inspection of Fig. 6 shows that the effect of SO_4 ⁼ ions can be distinguished from the effect of Ca and Mg.

MgCl₂ at $pmH_1 < 6.0$ obviously does not modify $k'^c_{(1)1}$ which is thus the same as in pure bicarbonate solutions at the same ionic strength. The ordinate difference between curves 3 and 4 in Fig. 6 shows but little variations over the pmH_1 interval considered and allows one to calculate $pk'^c_{(1)1}$ and $pk'^c_{(2)1}$. Thus for the investigated buffers (MgSO₄ 0.030, [HCO₃⁻] + [CO₃⁻] between 0.0025 and 0.09) $pk'^c_{(1)1} = 5.89$ and $pk'^c_{(2)1} = 9.49$ at $\mu = 0.75$ (see Fig. 2 and curve segment in Fig. 4); $pk'^m_{(1)1} = 5.89 - 0.005$ and $pk'^m_{(2)1} = 9.49 - 0.005$. The correction for the change of concentration scale is somewhat smaller than in pure NaCl solutions and is based on a total salt content of 36.4g and the corresponding density of sea water 1.025 at 22°C (13).

Effect of Ca and Mg and the apparent ionization functions $k''_{(1)}$ and $k''_{(2)}$.—The shape of the curves of

EFFECT of MgSO₄ MgCl₂ CaCl₂ Na₂SO₄ on -LOG [H] in CARBONATE and BICARBONATE BUFFERS

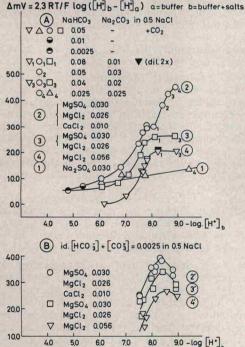


Fig. 6. Glass electrode emf shifts produced by the addition of MgSO₄, MgCl₂, CaCl₂, Na₂SO₄ to bicarbonate and carbonate buffers at atmospheric pressure. A. [HCO₃] + [CO₃=] 0.05 — 0.09 in 0.5 NaCl: Curve 1, effect of Na₂SO₄ (0.030); Curve 2, effect of MgSO₄ (0.030), MgCl₂ (0.026), and CaCl₂ (0.010). Precipitates are obtained at points 2, 3, and 4; result at pmH 4.8 corresponds to [HCO₃=] + [CO₃=] 0.0025; Curve 3, effect of MgSO₄ (0.030) and MgCl₂ (0.026); Curve 4, effect of MgCl₂ (0.056). B. [HCO₃-] + [CO₃=] = 0.0025. (2'), (3'), (4') same as (2), (3), (4).

Fig. 6 which give the emf shifts resulting from the addition of Ca and Mg salts to bicarbonate and carbonate buffers can be understood if one bears in mind that removing a constant amount of CO3= produces a pmH shift which is maximum at $pmH = \frac{1}{2}(pk'^m)$ + $pk'^{m}(2)$). When the trapped CO_3 is a function of the initial CO_3 concentration, the maximum is broadened and shifted toward a more alkaline pmH. Removing HCO_3^- produces no shift at $pm\dot{H} = \frac{1}{2}(pk'^m_{(1)} + pk'^m_{(2)})$, but results in an acidification or an alkalinization at more acid or more alkaline pmH values; HCO₃- trapping is evident in Fig. 6 in the acid range especially when CaCl2 is added to the more concentrated buffers already containing MgSO4 and MgCl₂, but the same operation produces a precipitate at pmH > 8.1. No precipitates are observed in the diluted buffers. The data gathered in Fig. 6 can be used to calculate the dissociation constants of MgCO3, CaCO3, MgHCO3+, and CaHCO3+ as Garrels et al. (12) have done from paH determinations on bicarbonate and carbonate buffers before and after addition of CaCl2 and MgCl2. This problem, which involves lengthy calculations, is quite beyond the scope of the present paper and will not be dealt with.

However, at $pmH_1 \ge 8.0$, Fig. 6 makes it possible to evaluate the apparent second ionization function of carbonic acid, $k''_{(2)}$, in presence of Ca⁺⁺, Mg⁺⁺, and SO₄= ions.

For buffers where [HCO₃⁻] + [CO₃⁻] = 0.0025, the emf shift due to the addition of 0.030 MgSO₄, 0.026 MgCl₂, and 0.010 CaCl₂ is equal to 38.0 mv at $pmH_1 \simeq 8.3$. With $pk'^c_{(2)1} = 9.67$ in the pure buffer, this leads to $pk''^c_{(2)1} = 9.67 - 0.65 = 9.02$ at $\mu = 0.73$; at $\mu = 0.75$, $pk''^c_{(2)1} = 9.015$.

More refined calculations taking into account the true ionization functions $k'^c_{(1)}$ (5.89) and $k'^c_{(2)}$ (9.49), the equilibrium $2\text{HCO}_3^- \Rightarrow \text{CO}_3^= + \text{H}_2\text{CO}_3$ which is displaced when CO_3^- is removed, give a mean value of 9.015 \pm 0.015 at $\mu=0.75$ in the $pm\text{H}_1$ interval 7.9-8.5, with a minimum at 8.3 where $pk''^c_{(2)1}=9.00$. On the molal scale $pk''^m_{(2)}=9.015-0.005$, again at $\mu=0.75$.

The agreement between the directly evaluated value of $pk''^c{}_{(2)1}$ and the calculated one, implies that, in first approximation, HCO_3^- -trapping by Mg^{++} and Ca^{++} must be very small at $pmH_1 \geq 8.0$. Trapping of HCO_3^- to a greater extent than Na ions do, would lead to an apparent lowering of $pk'^c{}_{(1)}$ and also affect $pk''^c{}_{(2)1}$ but in a more complicated way, depending on pH. This problem will not be discussed here, and it will be assumed that between pmH_1 7.9 and 8.5 it is not necessary to introduce a first apparent ionization function, or that $pk''^c{}_{(1)} = pk'^c{}_{(1)}$ in buffers where $[CO_3^-] + [HCO_3^-] = 0.0025$.

Since $pk''^{c}_{(2)1} - pk'^{c}_{(2)1} = 0.48$, $[CO_3^=]_T \simeq 3$ $[CO_3^=]$ and $[Mg - CaCO_3] \simeq 2$ $[CO_3^=]$. At pmH_1 8.0 $[HCO_3^-] + [CO_3^=] = 0.0025$, $[CO_3^=] = 7.34$ 10^{-5} , $[Mg - CaCO_3] = 1.45$ 10^{-4} or 0.22% of the total Ca and Mg concentrations, which is of the order of magnitude (0.28%) given by Garrels et al. (12, 15).

In buffers where $[CO_3^-] + [HCO_3^-] = 0.09$, $pk''^c_{(2)1}$ at pmH_1 8.1 is found equal to 9.12 when directly evaluated from curve 2, Fig. 6A, and equal to 9.10 when calculated at $\mu = 0.84$, taking reaction $2HCO_3^- \leftrightharpoons CO_3^- + H_2CO_3$ into consideration and neglecting the possibility of HCO_3^- trapping in the alkaline range. The apparent ionization function $pk''^c_{(2)1}$ is thus not only dependent on pH but also on the concentration of the buffering species. This remark is important and needs be taken into consideration when dealing with data to be valid in natural sea water.

True and apparent ionization functions of carbonic acid, in presence of Mg⁺⁺, Ca⁺⁺, and SO₄⁼, in NaCl solutions at 1000 kg. cm⁻² (μ = 0.75).—Comparison of curves 1 and 2 in Fig. 5 shows that ΔE_{1000} observed in pure buffer solutions is reduced by a constant amount in the presence of 0.030 Na₂SO₄, between pmH_1 6 and 9.5 (the reference 0.01 HCl + 0.49 NaCl solution has